Prof. Dr. Alfred Toth

Strukturdiagramme eigen- und kategorienrealer Relationen

1. Man kann die von Bense (1975, S. 37) eingeführte semiotische Matrix in eine Abbildungsmatrix transformieren und diese in der Form von kategorialen Übergängen (vgl. Toth 1997, S. 21 ff.) notieren:

	.1	.2	.3
1.	1.1	1.2	1.3
2.	2.1	2.2	2.3
3.	3.1	3.2	3.3

⇓

1. → .1	1. → .2	1. → .3
2. → .1	2. → .2	2. → .3
3. → .1	3. → .2	3. → .3

⇓

id_1	α	βα
α°	id_2	β
α°β°	β°	id_3

2. Damit sind wir soweit, daß wir die in Toth (2026) kategorial bestimmten eigen- und kategorienrealen Relationen auf die obige kategoriale Matrix abbilden[1] und die Distribution der Morphismen in der Form von Strukturdiagrammen darstellen können.

(1, 1, 1) $[id_1, id_1, id_1]$

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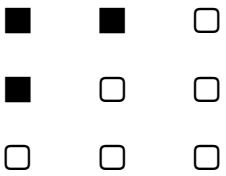
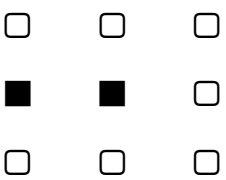
[1] Wir behalten die originale 3×3-Matrix bei und verzichten also auf die Abbildung von Multisets.

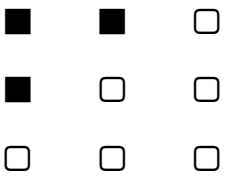
(1, 1, 2) $[\alpha^\circ, \mathrm{id}_1, \alpha]$



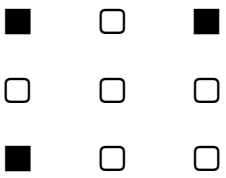
(1, 2, 1) $[\alpha^\circ, \mathrm{id}_2, \alpha^\circ]$



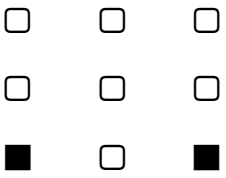
(2, 1, 1) $[\alpha, \mathrm{id}_1, \alpha^\circ]$



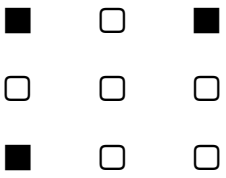
(1, 1, 3) $[\alpha^\circ\beta^\circ, \mathrm{id}_1, \beta\alpha]$



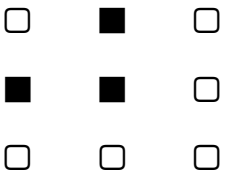
(1, 3, 1) $[\alpha^\circ\beta^\circ, \mathrm{id}_3, \alpha^\circ\beta^\circ]$



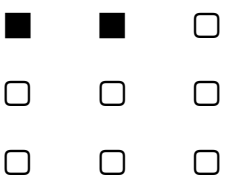
(3, 1, 1) $[\beta\alpha, \mathrm{id}_1, \alpha^\circ\beta^\circ]$



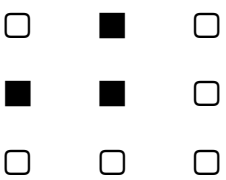
(1, 2, 2) $[\alpha^\circ, id_2, \alpha]$



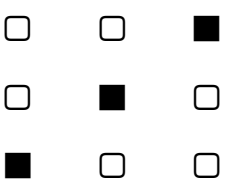
(2, 1, 2) $[\alpha, id_1, \alpha]$



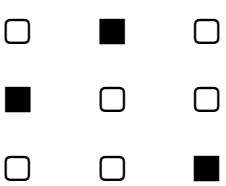
(2, 2, 1) $[\alpha, id_2, \alpha^\circ]$



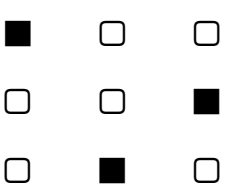
(1, 2, 3) $[\beta\alpha, id_2, \alpha^\circ\beta^\circ]$



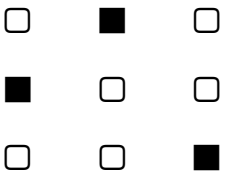
(1, 3, 2) $[\alpha, id_3, \alpha^\circ]$



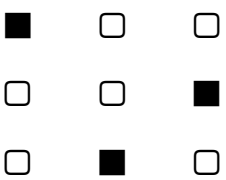
(2, 1, 3) $[\beta, id_1, \beta^\circ]$



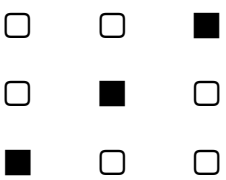
(2, 3, 1) $[\alpha^\circ, id_3, \alpha]$



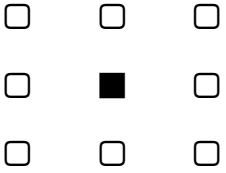
(3, 1, 2) $[\beta^\circ, id_1, \beta]$



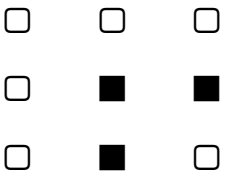
(3, 2, 1) $[\alpha^\circ\beta^\circ, id_2, \beta\alpha]$



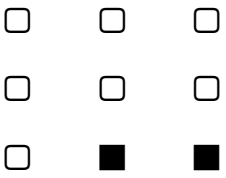
(2, 2, 2) $[id_2, id_2, id_2]$



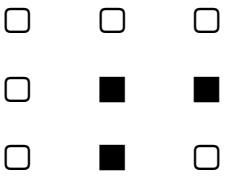
(2, 2, 3) $[\beta^\circ, id_2, \beta]$



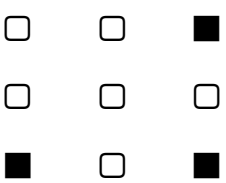
(2, 3, 2) $[\beta^\circ, id_3, \beta^\circ]$



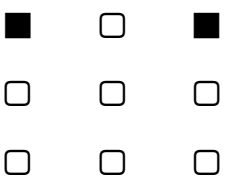
(3, 2, 2) $[\beta, id_2, \beta^\circ]$



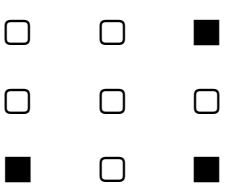
(1, 3, 3) $[\alpha^\circ\beta^\circ, id_3, \beta\alpha]$



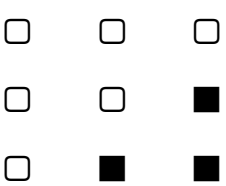
(3, 1, 3) $[\beta\alpha, id_1, \beta\alpha]$



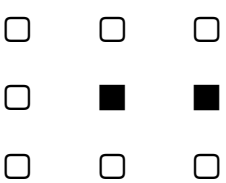
(3, 3, 1) $[\beta\alpha, id_3, \alpha^\circ\beta^\circ]$



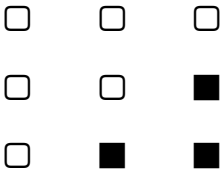
(2, 3, 3) $[\beta^\circ, id_3, \beta]$



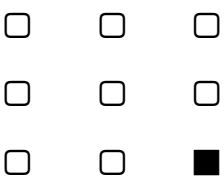
(3, 2, 3) $[\beta, id_2, \beta]$



(3, 3, 2) [β, id_3, β°]

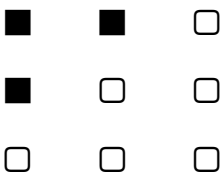


(3, 3, 3) [id_3, id_3, id_3]

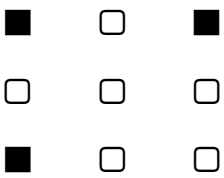


Die Abbildung der folgenden kategorialen Tripelrelationen auf Strukturdiagramme ist nicht-bijektiv:

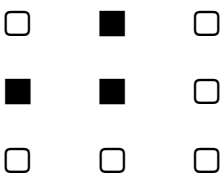
[α°, id_1, α], [α, id_1, α°]



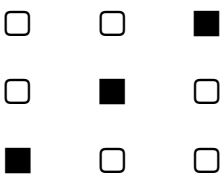
[α°β°, id_1, βα], [βα, id_1, α°β°]



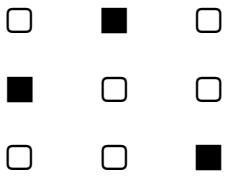
[α°, id_2, α], [α, id_2, α°]



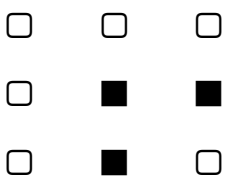
[βα, id_2, α°β°], [α°β°, id_2, βα]



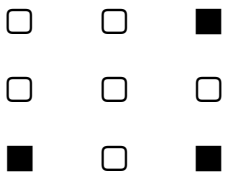
[α°, id_3, α], [β°, id_1, β]



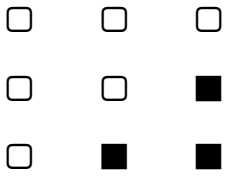
[β°, id_2, β], [β, id_2, β°]



[α°β°, id_3, βα], [βα, id_3, α°β°]



[β°, id_3, β], [β, id_3, β°]



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18.3.2026